

CREATING GRAPHICS FROM SCRATCH

CASE STUDIES

Till Tantau

Institute for Theoretical Computer Science
University Lübeck

GTEM Midterm Meeting 2008

OUTLINE

FIGURE 1: COMMUTATIVE DIAGRAM

The Figure and a Critique

Step 1: The Nodes

Step 2: The Edges

Step 3: Finishing Touches

FIGURE 2: A PIE CHART

The Figure and a Critique

Detail 1: Elliptical Arcs

Detail 2: Perpendicular Lines

Detail 3: Shadings

FIGURE 3: A CONSTRUCTION FROM EUCLID'S ELEMENTS

The Figure

Step 1: The Line AB

Step 2: The Circles

Step 3: The Intersection of the Circles

Step 4: Finishing Touches

particular D is regular over M . Also $\Delta \cap A = \Delta \cap \nu(A) = 1$, so $DE = D\hat{N} = \hat{N}E$.

$$\begin{array}{ccccccc}
 \hat{N} & \xrightarrow{\quad} & \hat{N}(y) & \xrightarrow{\quad} & \hat{N}E' & \xrightarrow{\quad} & \hat{N}E \\
 \downarrow & & \downarrow & & \downarrow & \nearrow D & \downarrow \\
 M & \xrightarrow{\quad} & M(y) & \xrightarrow{\quad} & E' & \xrightarrow{\quad} & E
 \end{array}$$

Choose a Galois ring cover \hat{S}/R of $\hat{N}E/M(y)$ [FJ05, Definition 6.1.3 and Remark 6.1.5] such that $y \in R$ and $x \in \hat{S}$. Let $U = \hat{S} \cap D$. The ring extension U/R corresponds to a dominating separable rational map $\text{Spec}(U) \rightarrow \text{Spec}(R)$. Since the quotient field of R is a rational function field, $\text{Spec}(R)$ is an open subvariety of an affine space. Therefore, by the definition of PAC extensions we have an M -epimorphism $\varphi: U \rightarrow M$ with $\alpha = \varphi(y) \in F$. The field D is regular over M and $D\hat{N} = \hat{N}E$, hence $\hat{S} = U \otimes_M \hat{N}$ [FJ05, Lemma 2.5.10]. Extend φ to an \hat{N} -epimorphism $\varphi: \hat{S} \rightarrow \hat{N}$. Then, φ induces a homomorphism $\varphi^*: \text{Gal}(M) \rightarrow \text{Gal}(\hat{N}E/D)$ which satisfies $\text{res}_{\hat{N}E, \hat{N}} \circ \varphi^* = \text{res}_{M, \hat{N}}$, where M_s is a separable closure of M [FJ05, Lemma 6.1.4]. Let ψ be the restriction of φ to $S = \hat{S} \cap E$. The equality $DE = \hat{N}E$ implies that \hat{S} is a subring of the quotient field of SU . Since $\psi(\hat{S}) = \hat{N}$ and $\psi(U) = M$ it follows that $\psi(S) = \hat{N}$ and $\psi^* = \text{res}_{\hat{N}E, E} \circ \varphi^*$. From the commutative diagram

$$\begin{array}{ccc}
 & & \text{Gal}(M) \\
 & \swarrow \psi^* & \downarrow \text{res} \\
 & \Delta & \text{Gal}(\hat{N}/M) \\
 \downarrow \text{res} & \nearrow \psi^* & \downarrow \text{res} \\
 \text{Gal}(E/E') & & \text{Gal}(\hat{N}/M)
 \end{array}$$

it follows that $(\psi^*)^{-1}(\nu(A_0)) = \text{res}_{M, \hat{N}}^{-1}(\text{Gal}(\hat{N}/N)) = \text{Gal}(N)$. Consequently, the residue field of $E'(x)$ under ψ is N . Also $E' \subseteq D$ implies that the residue field of E' is M . Consequently, $N = M(\beta)$, where $\beta = \psi(x)$ is a root of $f(X, \alpha)$. Finally, since $[N : M] = n$, the polynomial $f(X, \alpha)$ is irreducible over M .

To complete the proof we need to find infinitely many $\alpha \in F$ as above. This is done by the 'Rabinovich trick', that is, we replace R by the localization of R at $\prod_{i=1}^n (y - \alpha_i)$ (see [JR94, Remark 1.2(c)]). \square

Corollary 2. *Let M/F be a PAC extension, let $f(X, y) \in M[X, y]$ be a polynomial of degree n in X , and let N/M be a separable extension of degree n . Assume that the Galois*

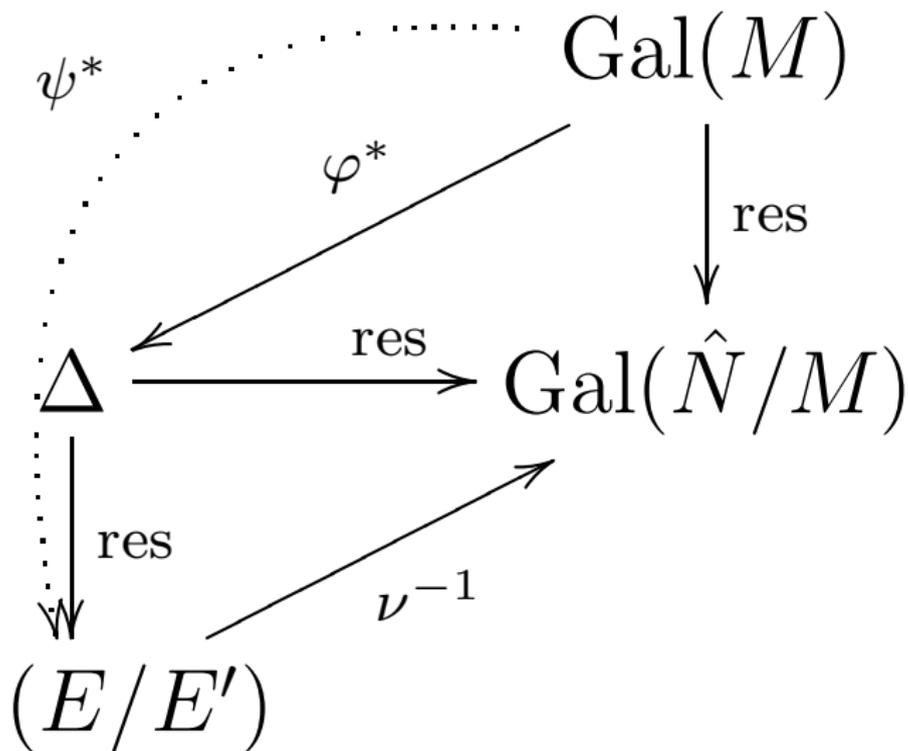


Bary-Soroker Lior

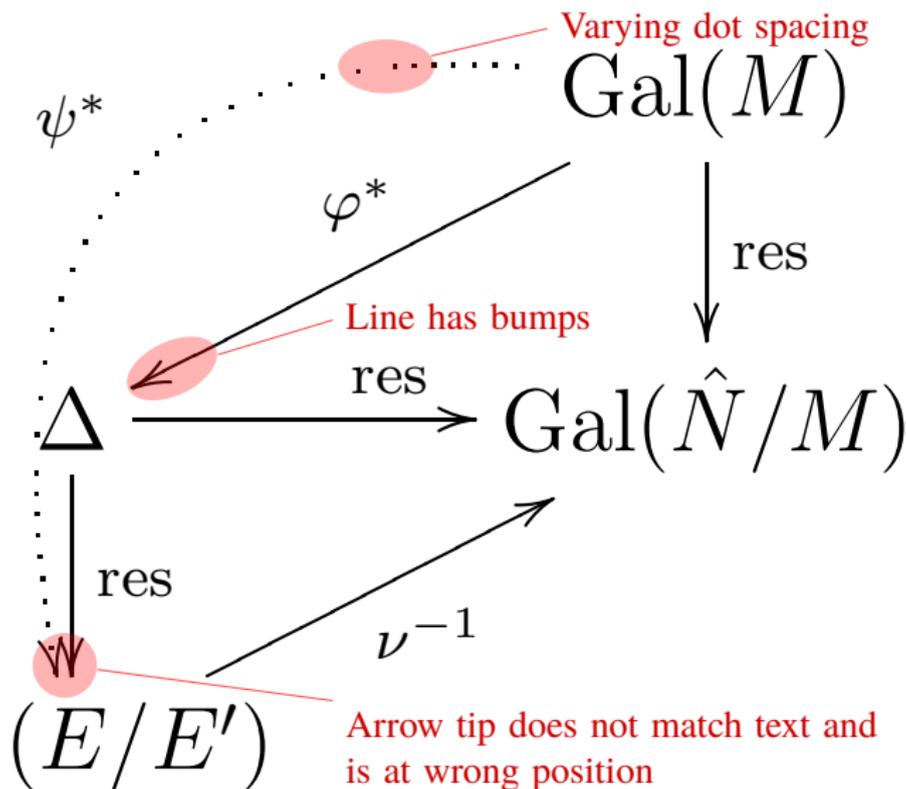
Dirichlet's Theorem For
Polynomial Rings

arXiv:math/0612801v2

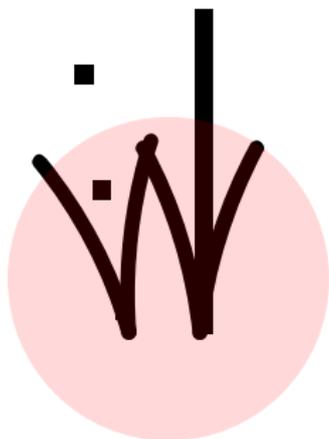
CLOSEUP OF THE FIGURE



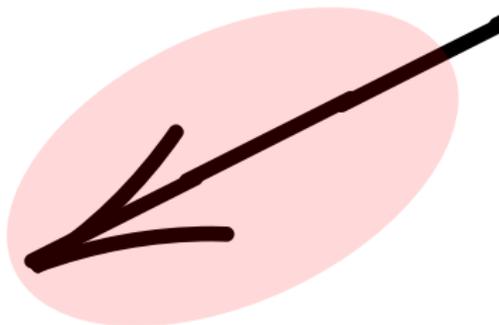
CRITIQUE



CLOSEUPS OF THE PROBLEMATIC AREAS.



Arrow tip does not match text and is at wrong position



Line has bumps

STEP 1: CREATING THE NODES.

BASIC IDEA

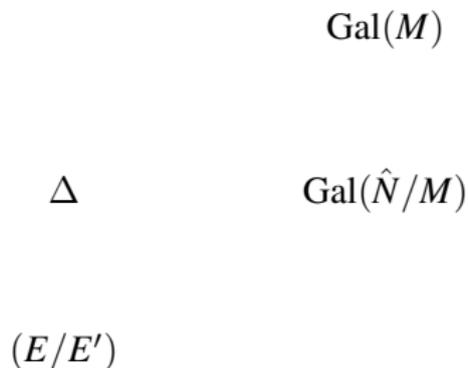
To (re)create the figure in TikZ, we start with the **nodes**, which are created using the `node` command.

SYNTAX OF THE NODE CREATION COMMAND

- ▶ Start with `\node`.
- ▶ Then comes a sequences of **options**.
- ▶ Options are given in square brackets, with two exceptions:
We can say `at` (coordinate) to specify a special place, where the node should go.
We can say (name) to assign a name to a node.
- ▶ The node ends with some text in curly braces.

STEP 1: CREATING THE NODES.

A SIMPLE PLACEMENT



```
\begin{tikzpicture}
  \node (EE) at (0,0) {$(E/E')$};
  \node (Delta) at (0,1.5) {$\Delta$};
  \node (GalNM) at (3,1.5) {$\mathrm{Gal}(\hat{N}/M)$};
  \node (GalM) at (3,3) {$\mathrm{Gal}(M)$};
\end{tikzpicture}
```

STEP 1: ALIGNING THE NODES

BASIC IDEA.

THE PROBLEM

Providing “hard-wired” coordinates like $(3, 1.5)$ is **problematic**:

- ▶ When you read the code, it is hard to tell, where something will go.
- ▶ When you change something later, you may need to change many such coordinates.
- ▶ It is hard to make sure that all spacings and alignments are correct.

POSSIBLE SOLUTIONS

- ▶ You can use options like `right=of Delta` to place a node relative to some other node.
- ▶ You can use a **TikZ-matrix**. It works like a \LaTeX matrix, only inside a picture.

STEP 1: ALIGNING THE NODES.

ALIGNMENT USING A MATRIX.

$\text{Gal}(M)$

Δ

$\text{Gal}(\hat{N}/M)$

(E/E')

```
\matrix[column sep=1cm,row sep=1cm]
{
    & \node (GalM)   {$\text{Gal}(M)$}; & \\
  \node (Delta) {$\Delta$}; & \node (GalNM) {$\text{Gal}(\hat{N}/M)$}; & \\
  \node (EE)    {$ (E/E') $}; & & \\
};
```

STEP 1: ALIGNING THE NODES.

SIMPLIFIED VERSION...

$\text{Gal}(M)$

Δ

$\text{Gal}(\hat{N}/M)$

(E/E')

```
\matrix [column sep=1cm,row sep=1cm,matrix of math nodes] (fig)
{
    & \mathrm{Gal}(M) & \\
    \Delta & \mathrm{Gal}(\hat{N}/M) & \\
    (E/E') & & \\
};
% Reference Gal(M) as (fig-1-2)
```

STEP 1: ALIGNING THE NODES.

... WITH ALTERNATE NAMING OF NODES.

$\text{Gal}(M)$

Δ

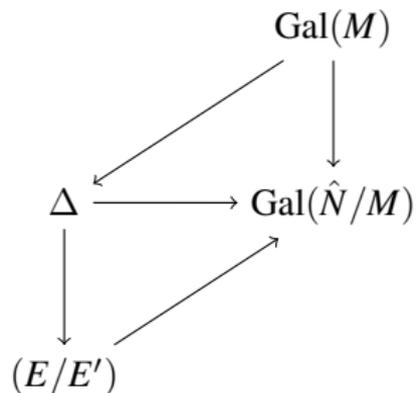
$\text{Gal}(\hat{N}/M)$

(E/E')

```
\matrix [column sep=1cm,row sep=1cm,matrix of math nodes]
{
      & |(M)| & \mathrm{Gal}(M) & \\
|(Delta)| \Delta & |(NM)| & \mathrm{Gal}(\hat{N}/M) & \\
|(EE)| & (E/E') & & \\
};
% Reference Gal(M) as (M)
```

STEP 2: CONNECTING THE NODES.

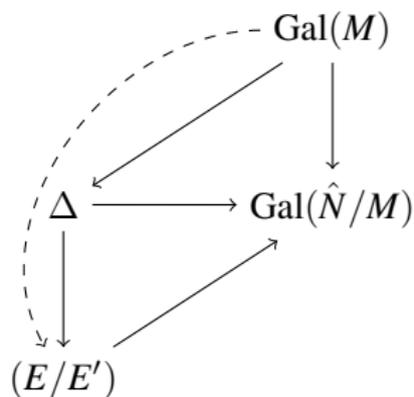
SIMPLE STRAIGHT LINE.



```
\matrix [column sep=1cm,row sep=1cm,matrix of math nodes]
{
    & |(M)| & \Gal(M) & \\
    |(Delta)| & \Delta & |(NM)| & \Gal(\hat{N}/M) \\
    |(EE)| & (E/E') & & \\
};
\draw (M) edge [->] (Delta)
      (M) edge [->] (NM)
      (Delta) edge [->] (NM)
      (EE) edge [->] (EE)
      (EE) edge [->] (NM);
```

STEP 2: CONNECTING THE NODES.

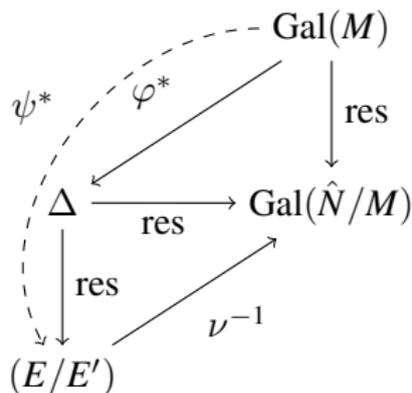
THE CURVED, DASHED LINE.



```
\draw (M)      edge [->] (Delta)
              edge [->] (NM)
              edge [->,dashed,out=180,in=120] (EE)
(Delta) edge [->] (NM)
              edge [->] (EE)
(EE)   edge [->] (NM);
```

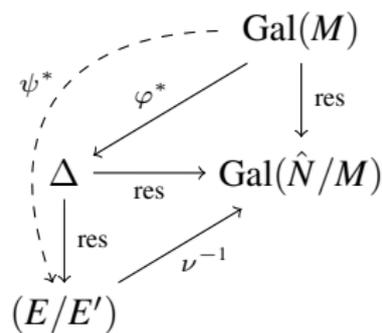
STEP 2: CONNECTING THE NODES.

ADDING THE LABELS



```
\draw [auto=right]
(M) edge [->] node {\varphi^*} (Delta)
edge [->] node [swap] {res} (NM)
edge [->,dashed,out=180,in=120]
node {\psi^*} (EE)
(Delta) edge [->] node {res} (NM)
edge [->] node [swap] {res} (EE)
(EE) edge [->] node {\nu^{-1}} (NM);
```

STEP 3: FINISHING TOUCHES

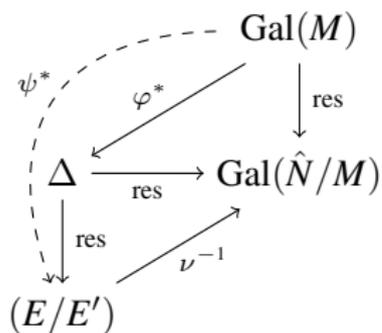
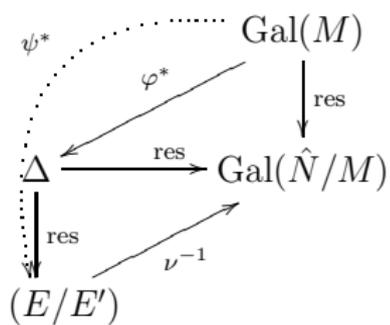


- ▶ Adjust “looseness” of the curve and dash phase.
- ▶ Reduce distance of φ^* , ψ^* and ν^{-1} to the line.
- ▶ Make edge labels smaller (as in $A \xrightarrow{X} B$)

THE COMPLETE CODE.

```
\begin{tikzpicture}
  \matrix [column sep=7mm,row sep=7mmm,matrix of math nodes]
  {
    & |(M)| & \Gal(M) & \\
    |(Delta)| & \Delta & |(NM)| & \Gal(\hat N/M) \\
    |(EE)| & (E/E') & & \\
  };
  \draw [auto=right,nodes={font=\scriptsize}]
    (M) edge [->] node [inner sep=0pt] {$\varphi^*$} (Delta)
        edge [->] node [swap] {res} (NM)
        edge [->,out=180,in=110,looseness=1.4,
              dashed,dash phase=3pt]
          node [inner sep=0pt] {$\psi^*$} (EE)
    (Delta) edge [->] node {res} (NM)
             edge [->] node [swap] {res} (EE)
    (EE) edge [->] node [inner sep=0pt] {$\nu^{-1}$} (NM);
\end{tikzpicture}
```

COMPARISON OF ORIGINAL AND REWORKED FIGURE.

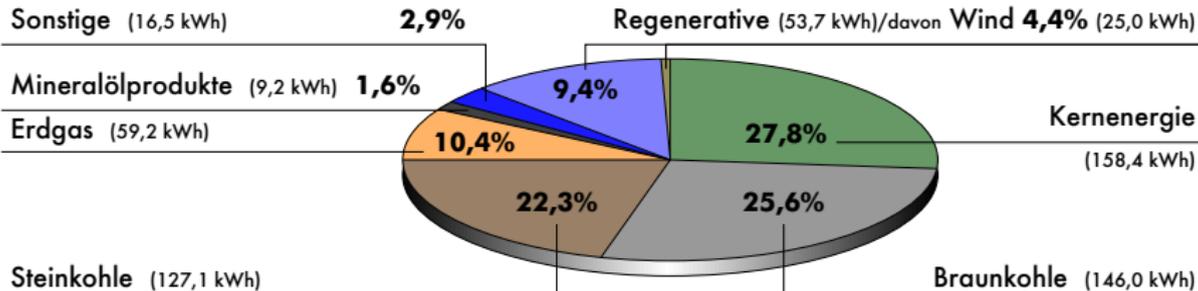


A FIGURE FROM A MAJOR GERMAN NEWSPAPER.

Kohle ist am wichtigsten

Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)

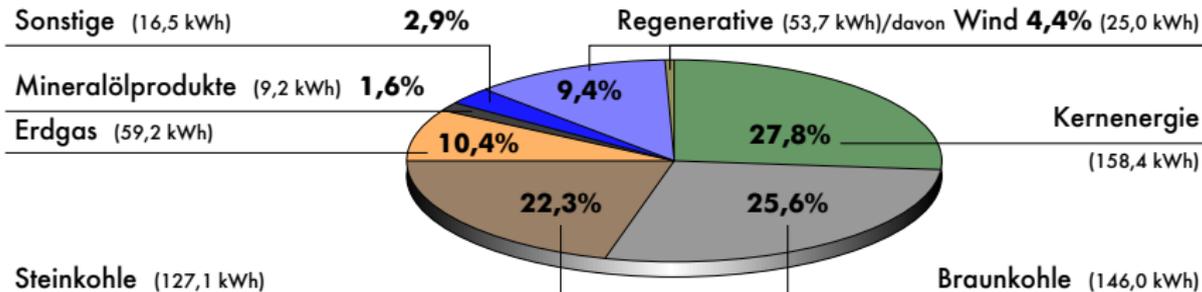


This figure is a redrawing of a figure from “Die Zeit,” June 4th, 2005.

CRITIQUE.

Kohle ist am wichtigsten Energemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)



- ▶ Coloring is random and misleading.
- ▶ Pie slice sizes do not reflect percentages.
- ▶ Main message is lost since coal is split across page.

DETAIL 1: PIE SLICES ARE ELLIPTIC ARCS.

Kohle ist am wichtigsten

Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)

Sonstige (16,5 kWh)

2,9%

Regenerative (53,7 kWh)/davon Wind 4,4% (25,0 kWh)

Mineralölprodukte (9,2 kWh)

1,6%

9,4%

Erdgas (59,2 kWh)

10,4%

Kernenergie

(158,4 kWh)

Steinkohle (127,1 kWh)

22,3%

25,6%

Braunkohle (146,0 kWh)

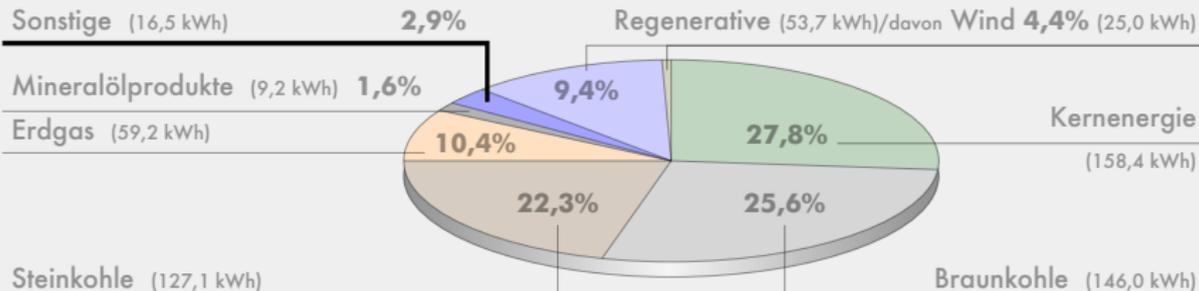
```
\fill[green!20!gray] (0,0) -- (90:1.2cm)
arc (90:-5:3.2cm and 1.2cm)
-- cycle;
```

DETAIL 2: A HORIZONTAL/VERTICAL JUNCTION.

Kohle ist am wichtigsten

Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)



```
\draw[very thick] (-22mm,7mm) |- (-80mm,14mm);
```

DETAIL 3: THE SHADING IN THE PIE CHART.

Kohle ist am wichtigsten

Energiemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)

Sonstige (16,5 kWh)

2,9%

Regenerative (53,7 kWh)/davon Wind 4,4% (25,0 kWh)

Mineralölprodukte (9,2 kWh) 1,6%

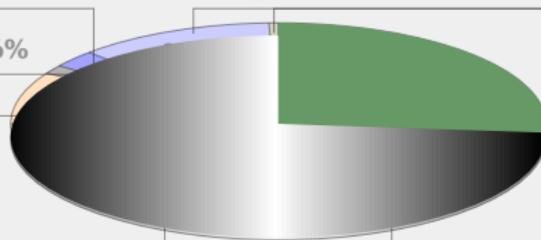
Erdgas (59,2 kWh)

Kernenergie

(158,4 kWh)

Steinkohle (127,1 kWh)

Braunkohle (146,0 kWh)



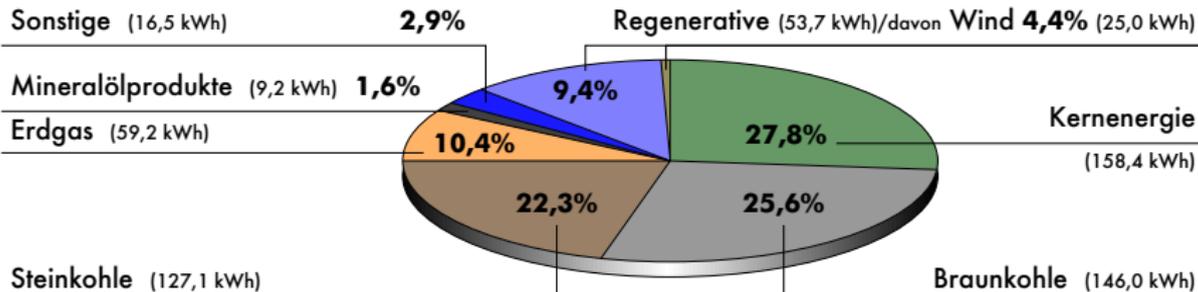
```
\shade [left color=black,right color=black,middle color=white]  
(0mm,-1.5mm) ellipse (3.2cm and 1.2cm);
```

```
\fill[green!20!gray] (0,0) -- (90:1.2cm)  
arc (90:-5:3.2cm and 1.2cm)  
-- cycle;
```

THE COMPLETE FIGURE.

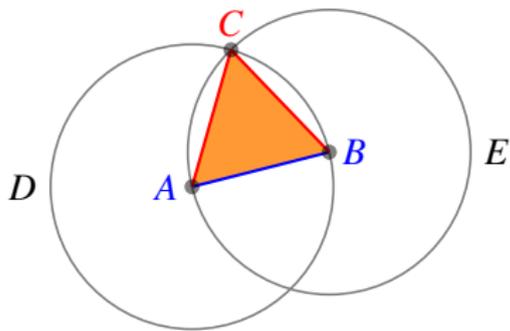
Kohle ist am wichtigsten Energemix bei der deutschen Stromerzeugung 2004

Gesamte Netto-Stromerzeugung in Prozent, in Milliarden Kilowattstunden (Mrd. kWh)



The complete figure can be constructed in this way.

A GEOMETRICAL CONSTRUCTION



Euclid of Alexandria
Proof of Proposition I
Elements, Book I

STEP 1: THE LINE *AB*

A SIMPLE LINE



```
\begin{tikzpicture}
  \coordinate (A) at (0,0);
  \coordinate (B) at (1.25,0.25);

  \draw[blue] (A) -- (B);
\end{tikzpicture}
```

- ▶ The `\coordinate` command is a shorthand for the `\node` command with empty text.

STEP 1: THE LINE AB

ADDING LABELS



```
\begin{tikzpicture}
  \coordinate [label=left:\textcolor{blue}{ $A$ }]
    (A) at (0,0);

  \coordinate [label=right:\textcolor{blue}{ $B$ }]
    (B) at (1.25,0.25);

  \draw[blue] (A) -- (B);
\end{tikzpicture}
```

- ▶ The `label` option makes it easy to add some text **around** an **another** node.
- ▶ Alternatively, one could explicitly create a node later on.

STEP 1: THE LINE AB

PERTURBED POSITIONS



```
\usetikzlibrary{calc}
\begin{tikzpicture}
  \coordinate [label=left:\textcolor{blue}{A}]
    (A) at ($ (0,0) + .1*(rand,rand) $);

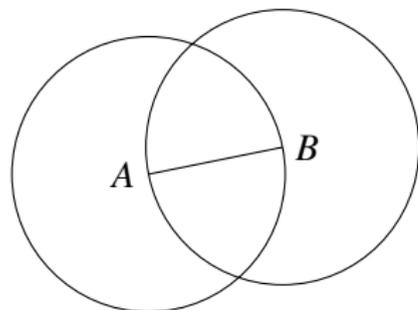
  \coordinate [label=right:\textcolor{blue}{B}]
    (B) at ($ (1.25,0.25) + .1*(rand,rand) $);

  \draw[blue] (A) -- (B);
\end{tikzpicture}
```

- Between ($\$$ and $\$$) you can do some **basic linear algebra on coordinates**.

STEP 2: THE CIRCLES

USING THE LET OPERATION



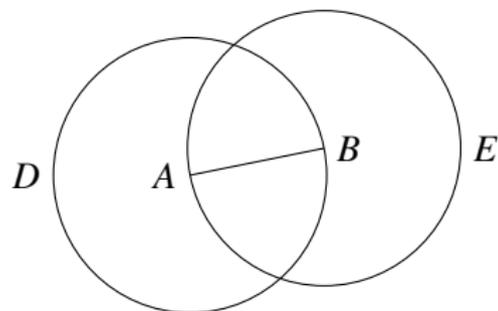
...

```
\draw (A) -- (B);
```

```
\draw let
  \p1          = ($ (B) - (A) $)
in
  (A) circle ({sqrt(\x1*\x1+\y1*\y1)})
  (B) circle ({sqrt(\x1*\x1+\y1*\y1)});
```

STEP 2: THE CIRCLES

USING THE THROUGH LIBRARY



```
\usetikzlibrary{through}
```

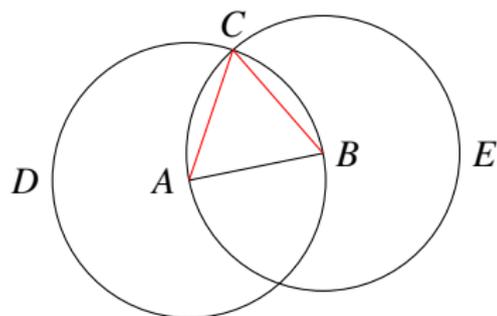
```
...
```

```
\draw (A) -- (B);
```

```
\node at (A) [draw,circle through=(B),label=left:$D$] {};
```

```
\node at (B) [draw,circle through=(A),label=right:$E$] {};
```

STEP 3: THE INTERSECTION OF THE CIRCLES

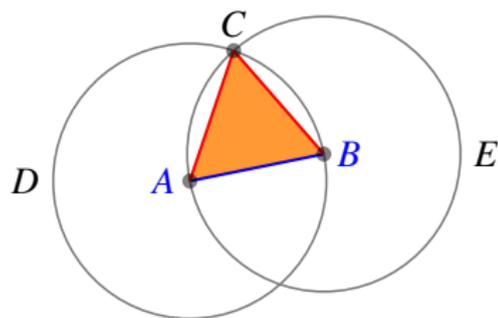


```
\usetikzlibrary{intersections}
...
\draw (A) -- (B);
\node at (A) [name path=D,draw,circle through=(B),label=...] {};
\node at (B) [name path=E,draw,circle through=(A),label=...] {};

\node [name intersections={of=D and E, by=C}]
  at (C) [above] {$C$};

\draw [red] (A) -- (C) (B) -- (C);
```

STEP 4: FINISHING TOUCHES



- ▶ Add **transparent circles** at the points *A*, *B*, and *C*.
- ▶ Fill triangle, but on the **background layer**.

THE COMPLETE CODE

```
\begin{tikzpicture}[thick,
    help lines/.style={semithick,draw=black!50}]
  \coordinate [label=left:\textcolor{blue}{{$A$}}]
    (A) at ($ (0,0) + .1*(rand,rand) $);
  \coordinate [label=right:\textcolor{blue}{{$B$}}]
    (B) at ($ (1.25,0.25) + .1*(rand,rand) $);
  \draw [blue] (A) -- (B);

  \node at (A) [circle through=(B),name path=D,
    help lines,draw,label=left:$D$] {};
  \node at (B) [circle through=(A),name path=E,
    help lines,draw,label=right:$E$] {};

  \node [name intersections={of=D and E, by=C}]
    at (C) [above] {{$C$}};
  \draw [red] (A) -- (C) (B) -- (C);

  \foreach \point in {A,B,C}
    \fill [black,opacity=.5] (\point) circle (2pt);

  \begin{pgfonlayer}{background}
    \fill[orange!80] (A) -- (C) -- (B) -- cycle;
  \end{pgfonlayer}
\end{tikzpicture}
```