



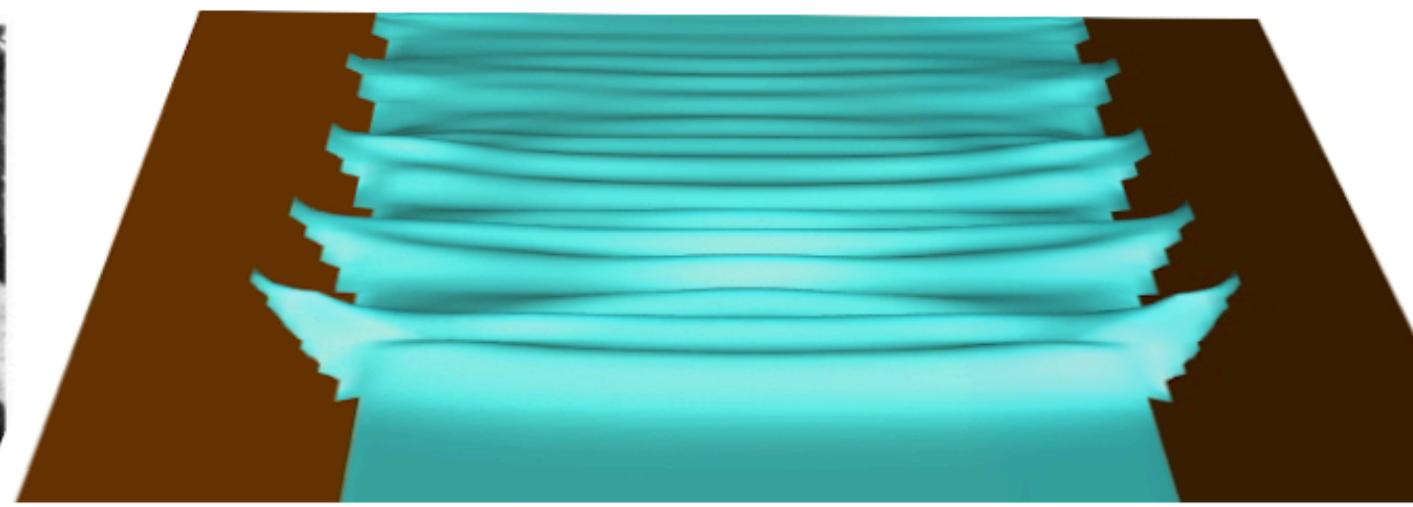
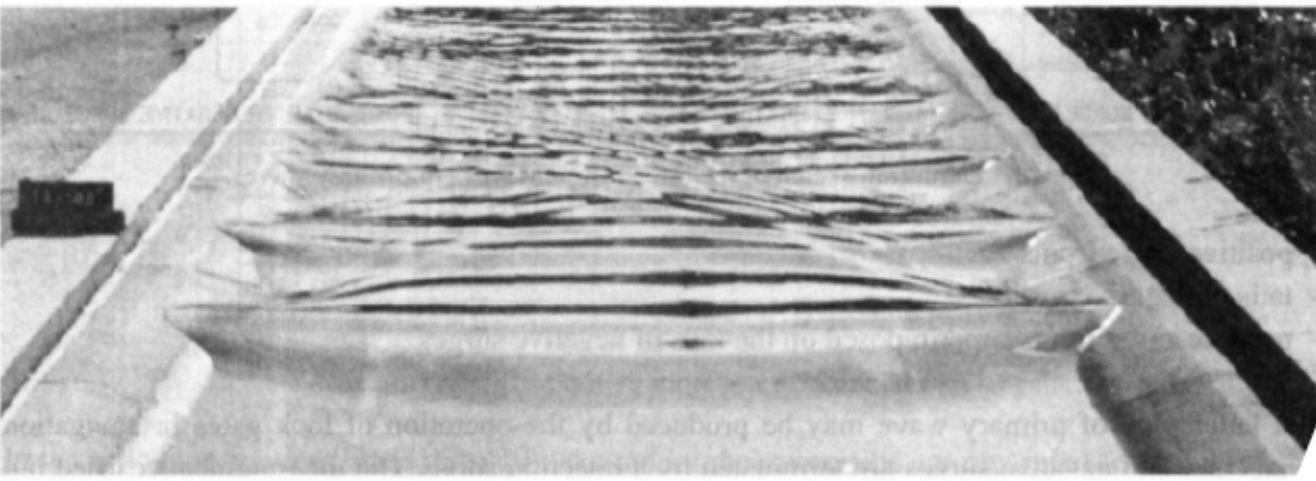
# Cardamom

**Lookout on possible evolutions:**

some MOR for small scales and in embedded moving domains

# Certified Adaptive discRete moDels for robust simulAtions of coMplex fLOws with Moving fronts

$Fr = 1.17$



## Approximate/asymptotic large scale modeling

$$\vec{\psi} + \alpha \mu^2 \nabla (h^2 \nabla \cdot \vec{\psi}) = \vec{Q}(h, \vec{u})$$

$$\partial_t \zeta + \nabla \cdot (h \vec{u}) = 0$$

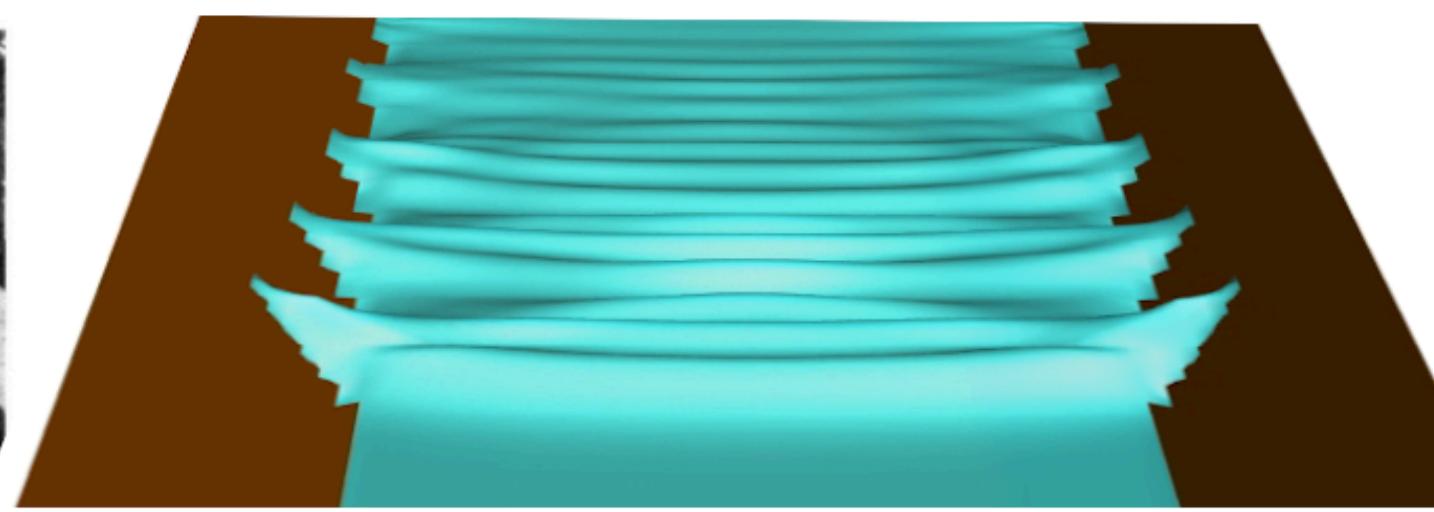
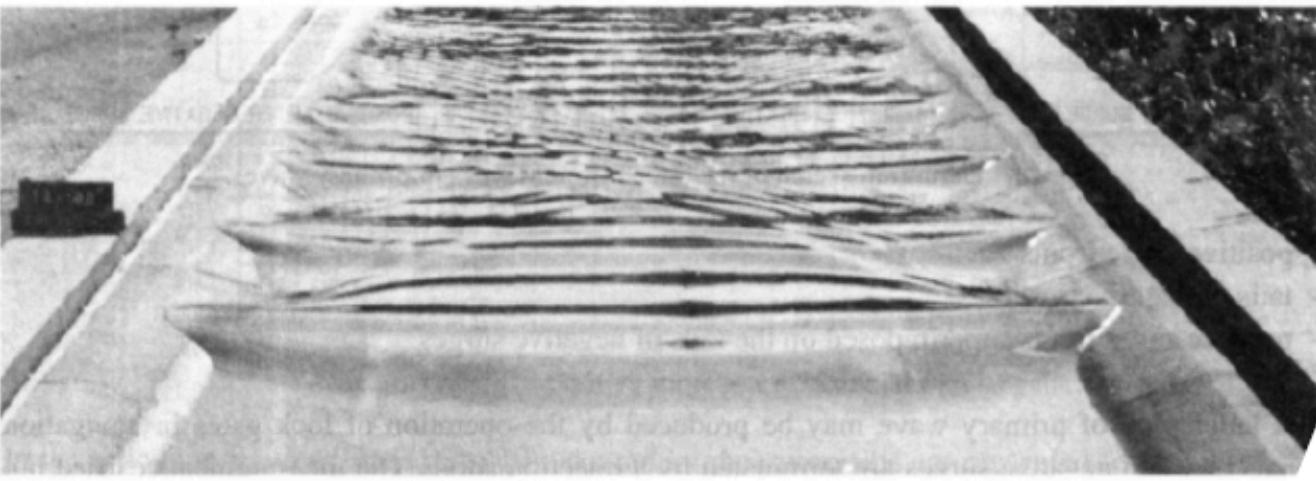
**Modeling error** (PDE analysis)

$$\partial_t (h \vec{u}) + \nabla \cdot (h \vec{u} \otimes \vec{u}) + c^2 \nabla \zeta = \mu^2 \vec{\psi} + \boxed{\mathcal{O}(\mu^4)}$$

$$\mu = \frac{\text{depth}}{\text{wavelength}}$$

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## Approximate/asymptotic large scale modeling

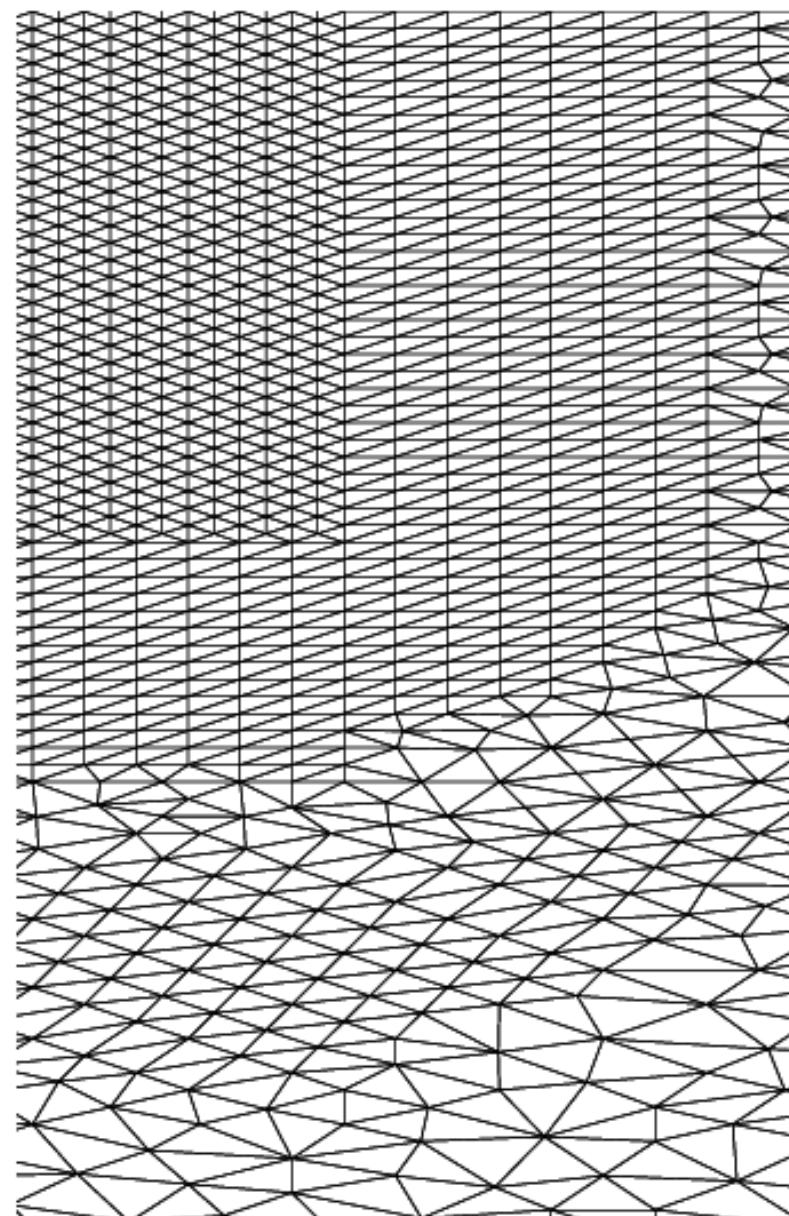
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$$\partial_t \zeta + \nabla \cdot (h \vec{u}) = 0$$

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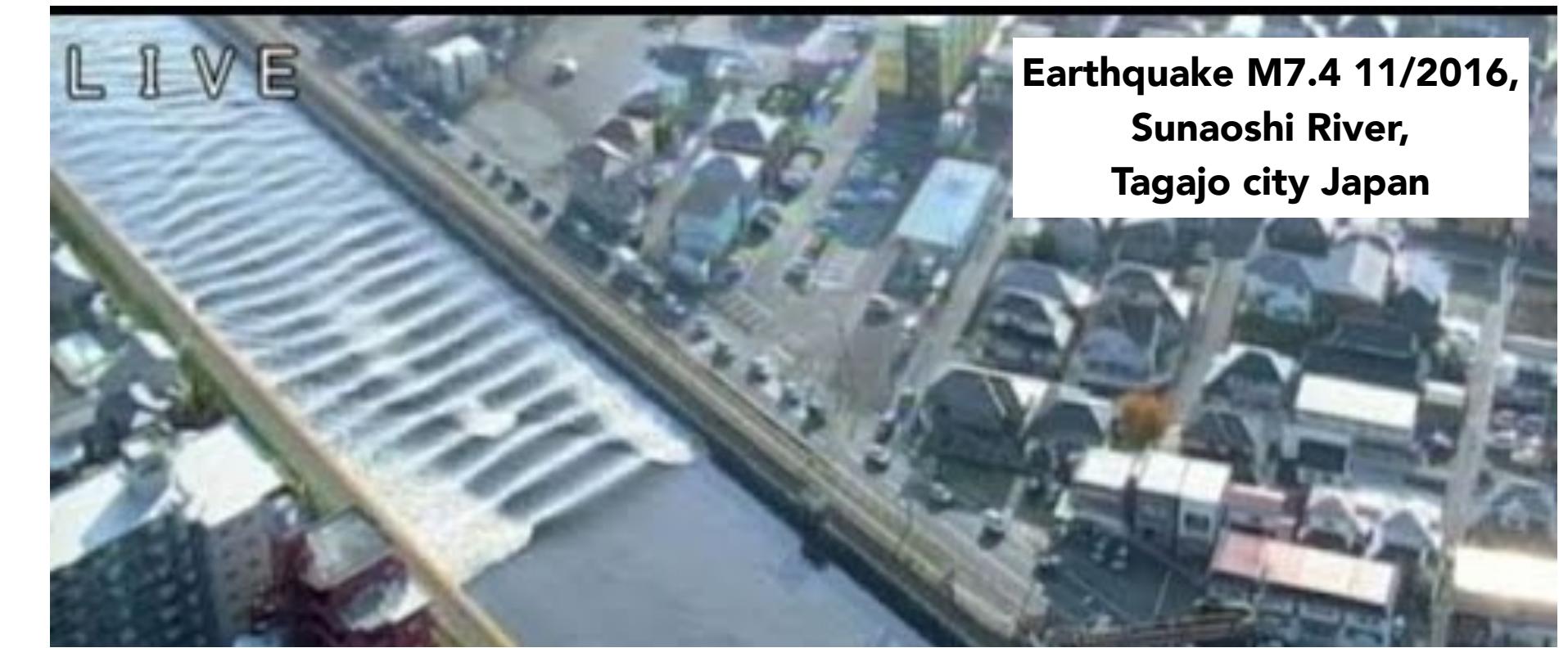
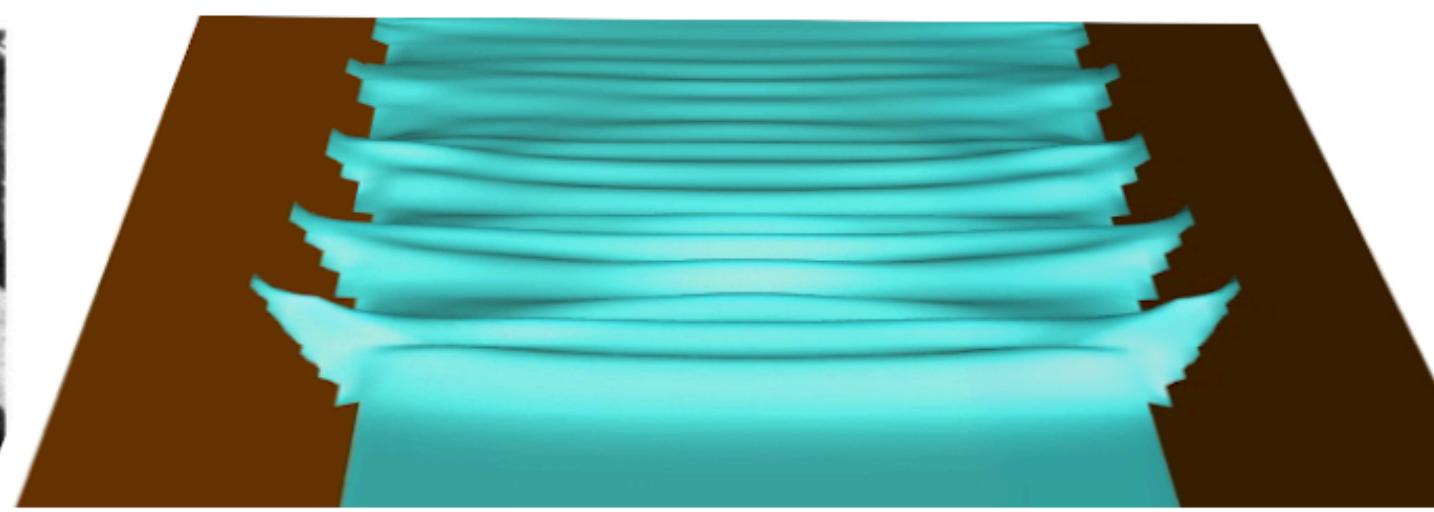
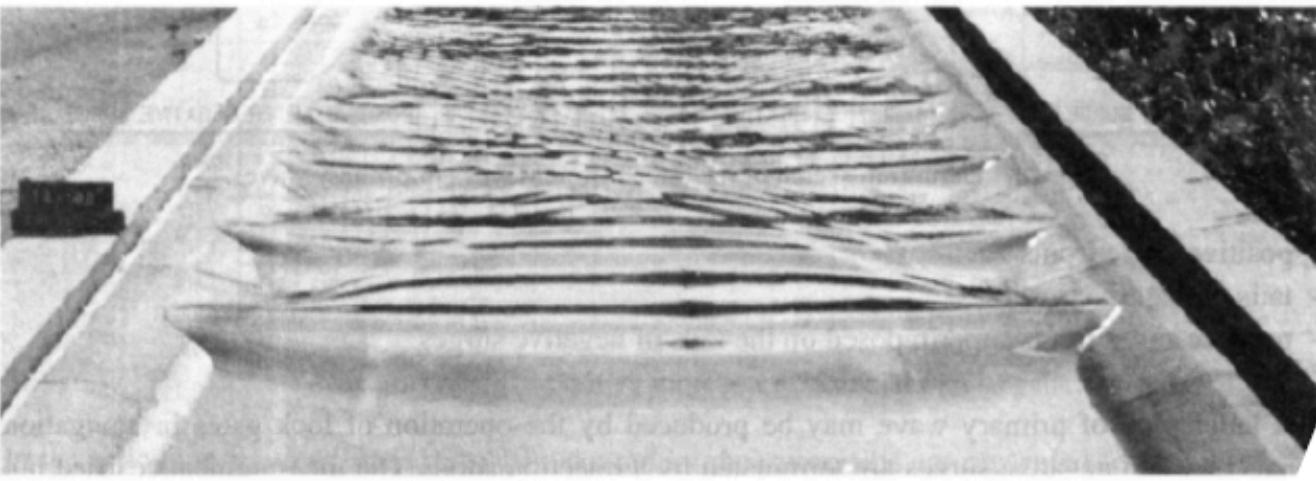
$$\partial_t (h \vec{u}) + \nabla \cdot (h \vec{u} \otimes \vec{u}) + c^2 \nabla \zeta = \mu^2 \vec{\psi} + \boxed{\mathcal{O}(\mu^4)} + \boxed{\mathcal{O}(\Delta x^p)}$$

**Discretization error** (Numerical analysis)



# Certified Adaptive discRete moDels for robust simulAtions of coMplex fLOws with Moving fronts

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## Approximate/asymptotic large scale modeling

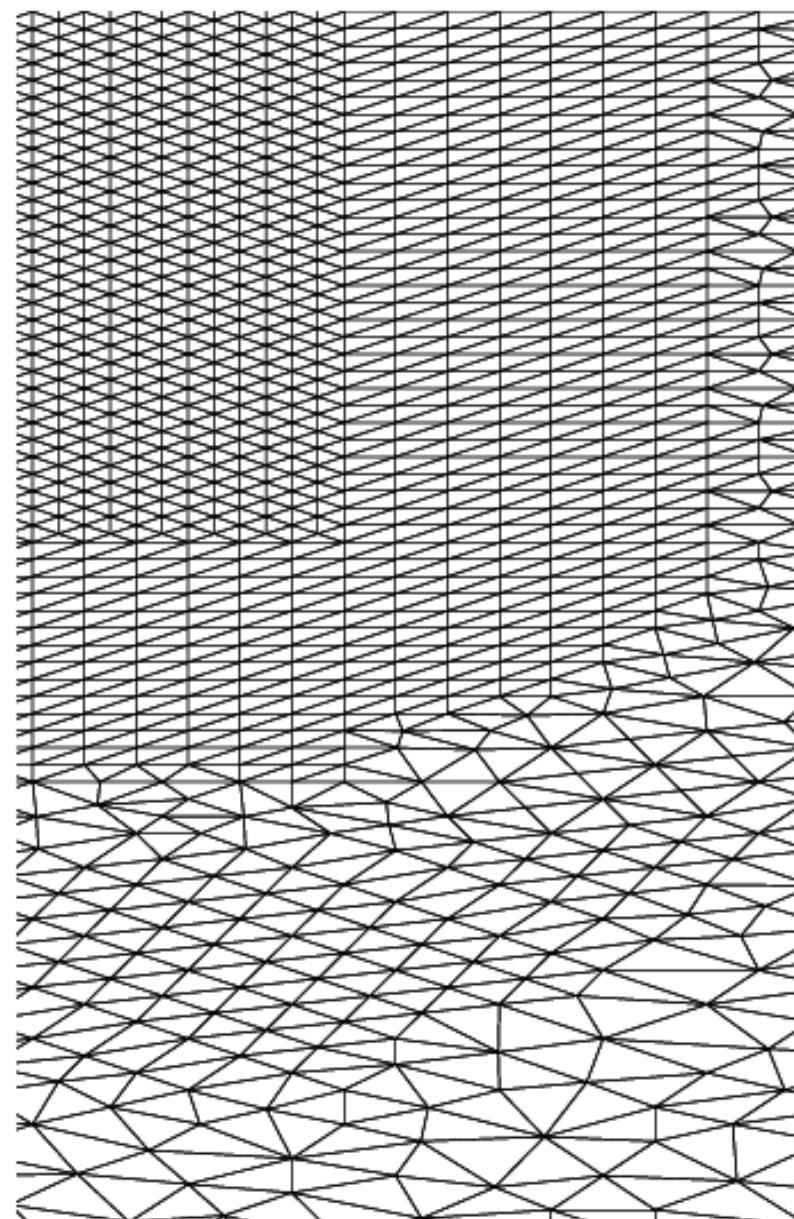
$$\vec{\psi} + \alpha \mu^2 \nabla (h^2 \nabla \cdot \vec{\psi}) = \vec{Q}(h, \vec{u})$$

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**Modeling error** (PDE analysis)

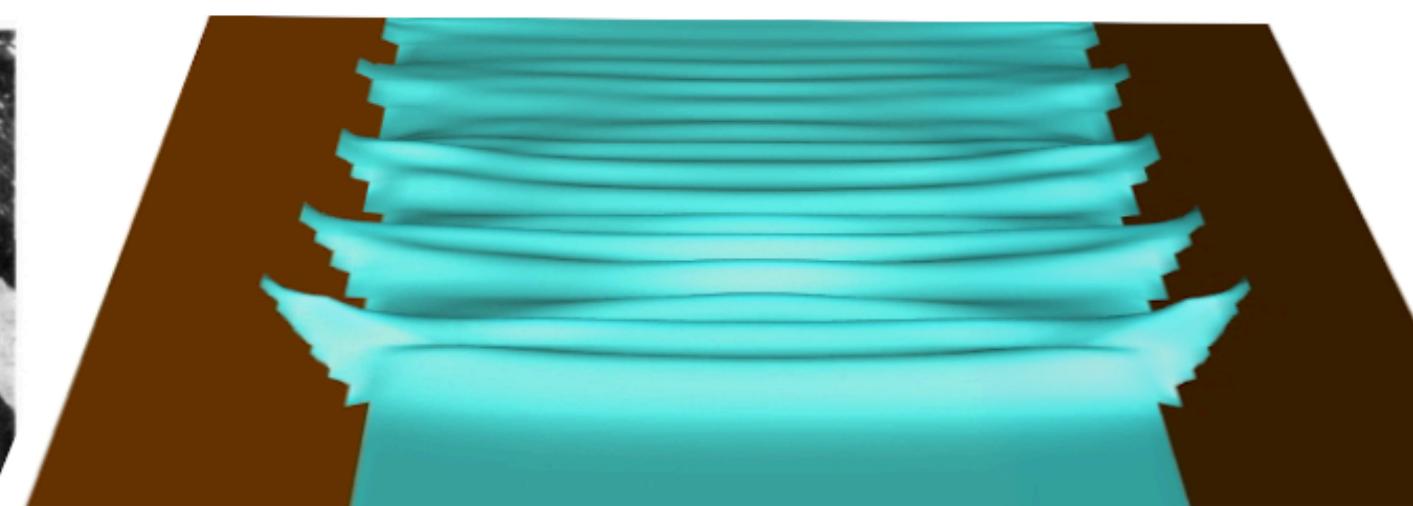
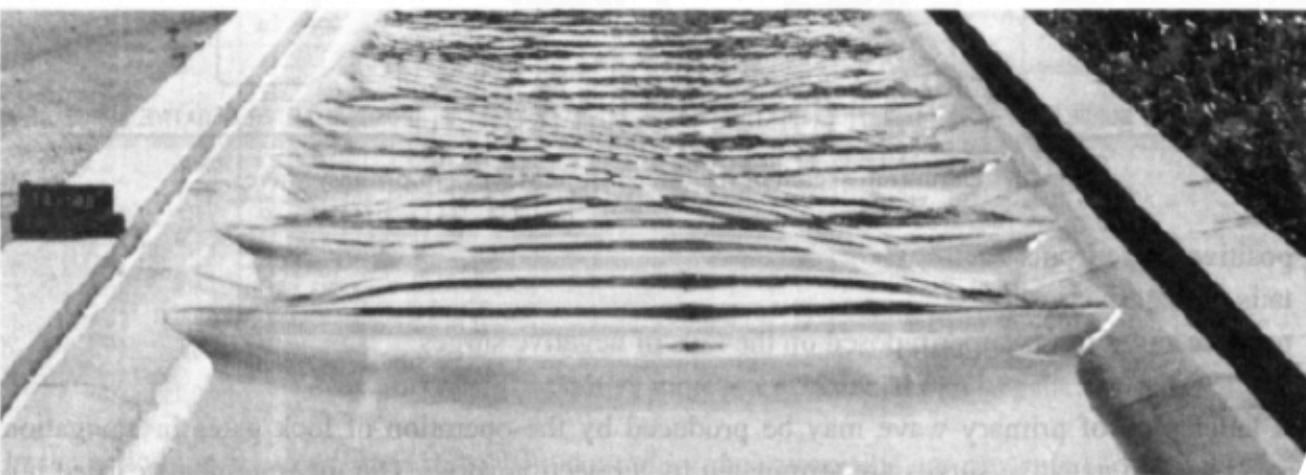
$$\partial_t (h \vec{u}) + \nabla \cdot (h \vec{u} \otimes \vec{u}) + c^2 \nabla \zeta = \mu^2 \vec{\psi} + \mathcal{O}(\mu^4) + \mathcal{O}(\Delta x^p)$$

**Discretization error** (Numerical analysis)

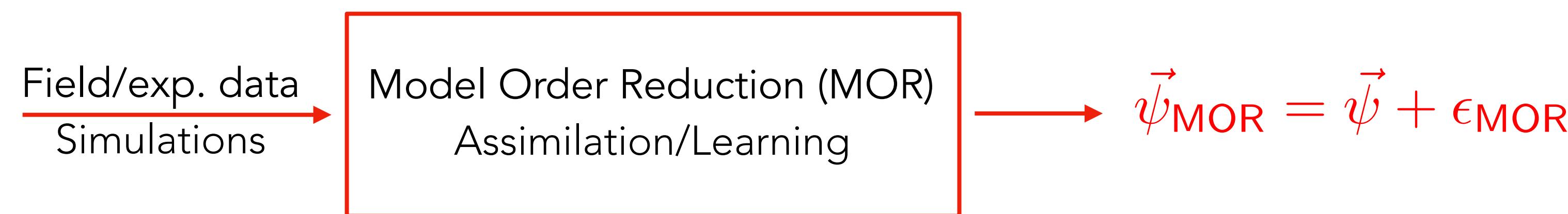


# Certified Adaptive discRete moDels for robust simulAtions of coMplex fLOws with Moving fronts

$Fr = 1.17$



## Approximate/asymptotic large scale modeling



$$\partial_t \zeta + \nabla \cdot (h \vec{u}) = 0$$

**Modeling error** (PDE analysis)

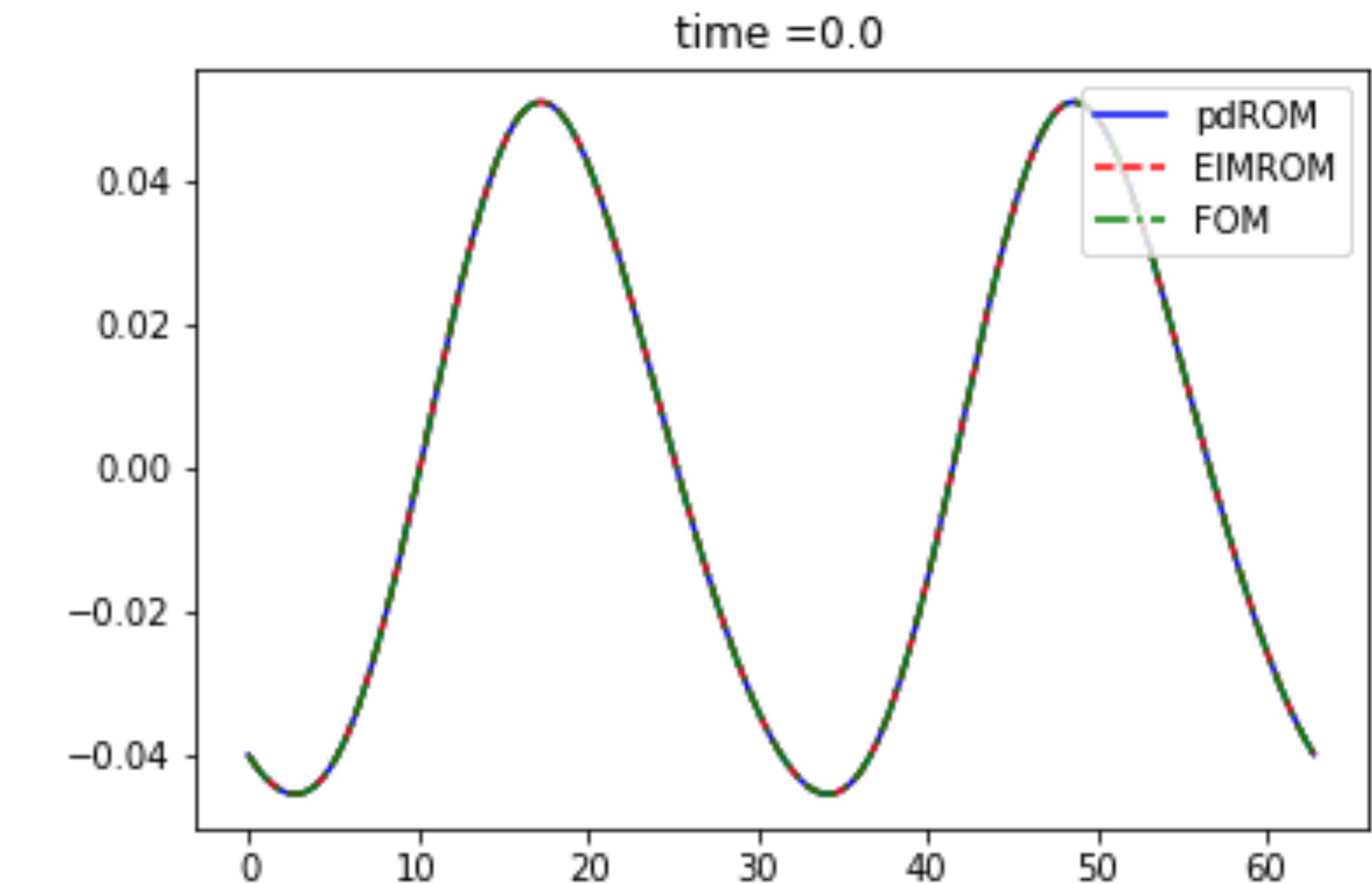
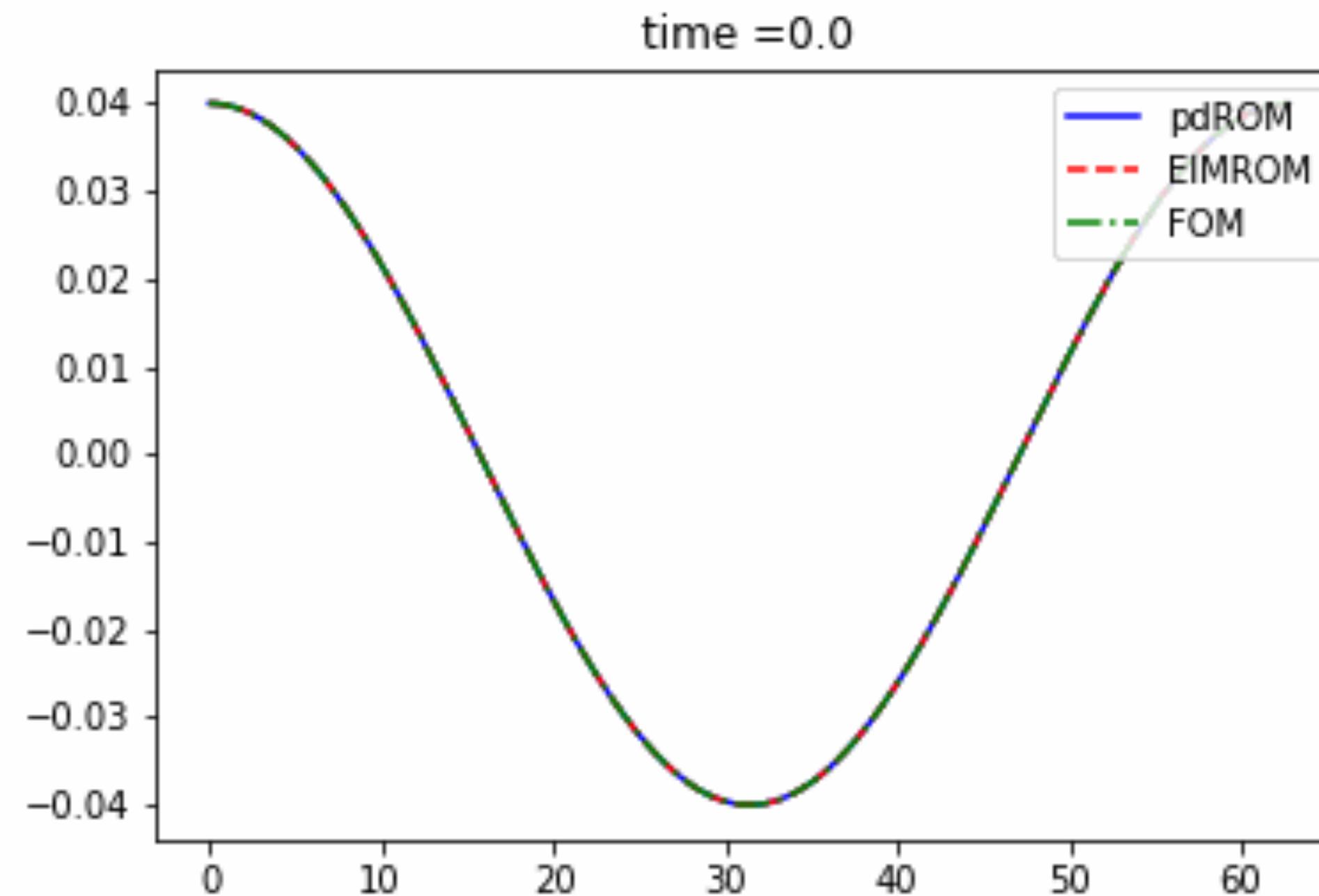
$$\partial_t (h \vec{u}) + \nabla \cdot (h \vec{u} \otimes \vec{u}) + c^2 \nabla \zeta = \mu^2 \vec{\psi} + \mathcal{O}(\mu^4) + \mathcal{O}(\Delta x^p) + \mathcal{O}(\mu^2 \epsilon_{\text{MOR}})$$

**Discretization error** (Numerical analysis)

# Certified Adaptive discRete moDels for robust simulAtions of coMplex fLOws with Moving fronts

KdV/BBM model: **PDE-ROM vs ROM**

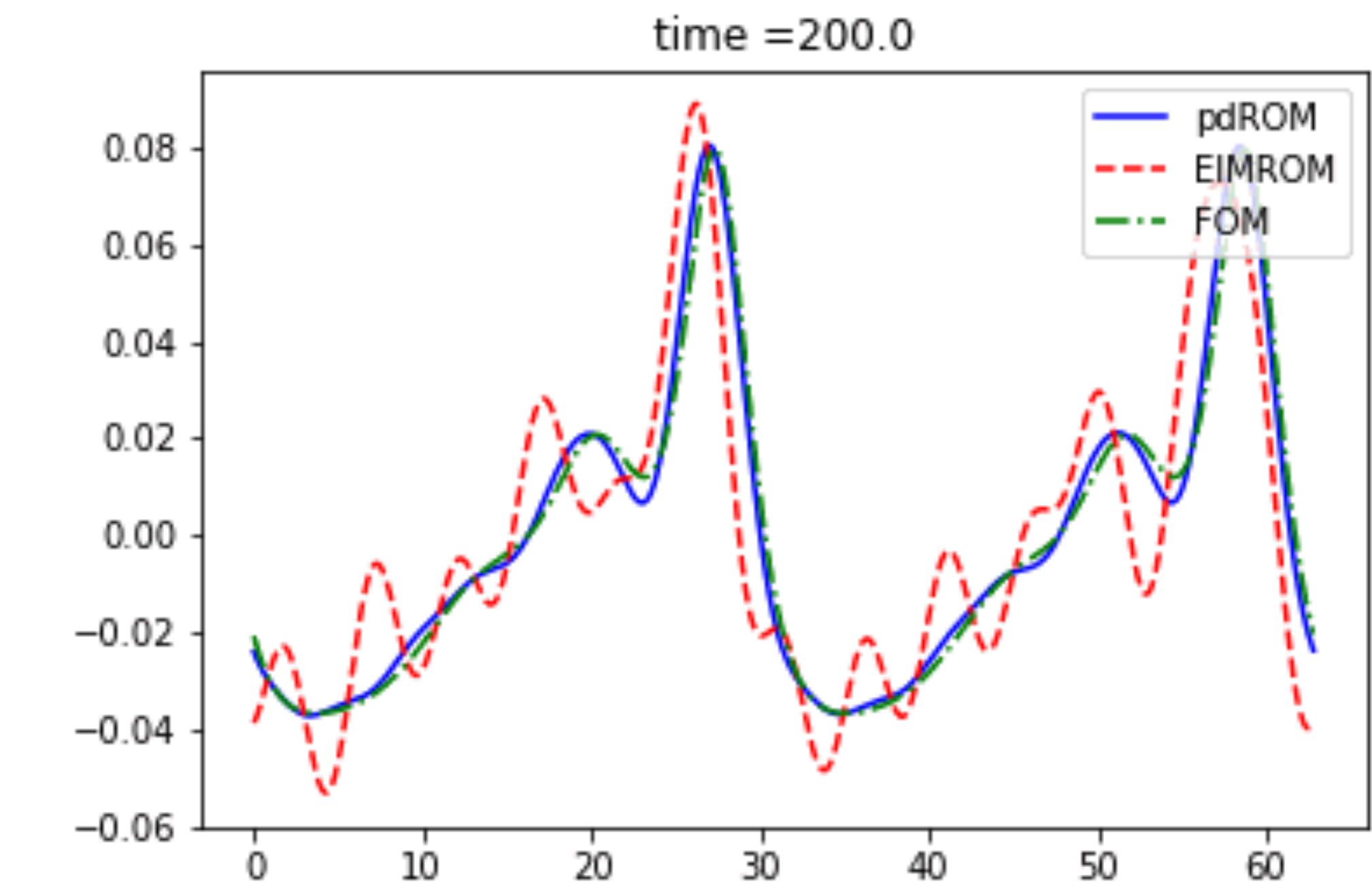
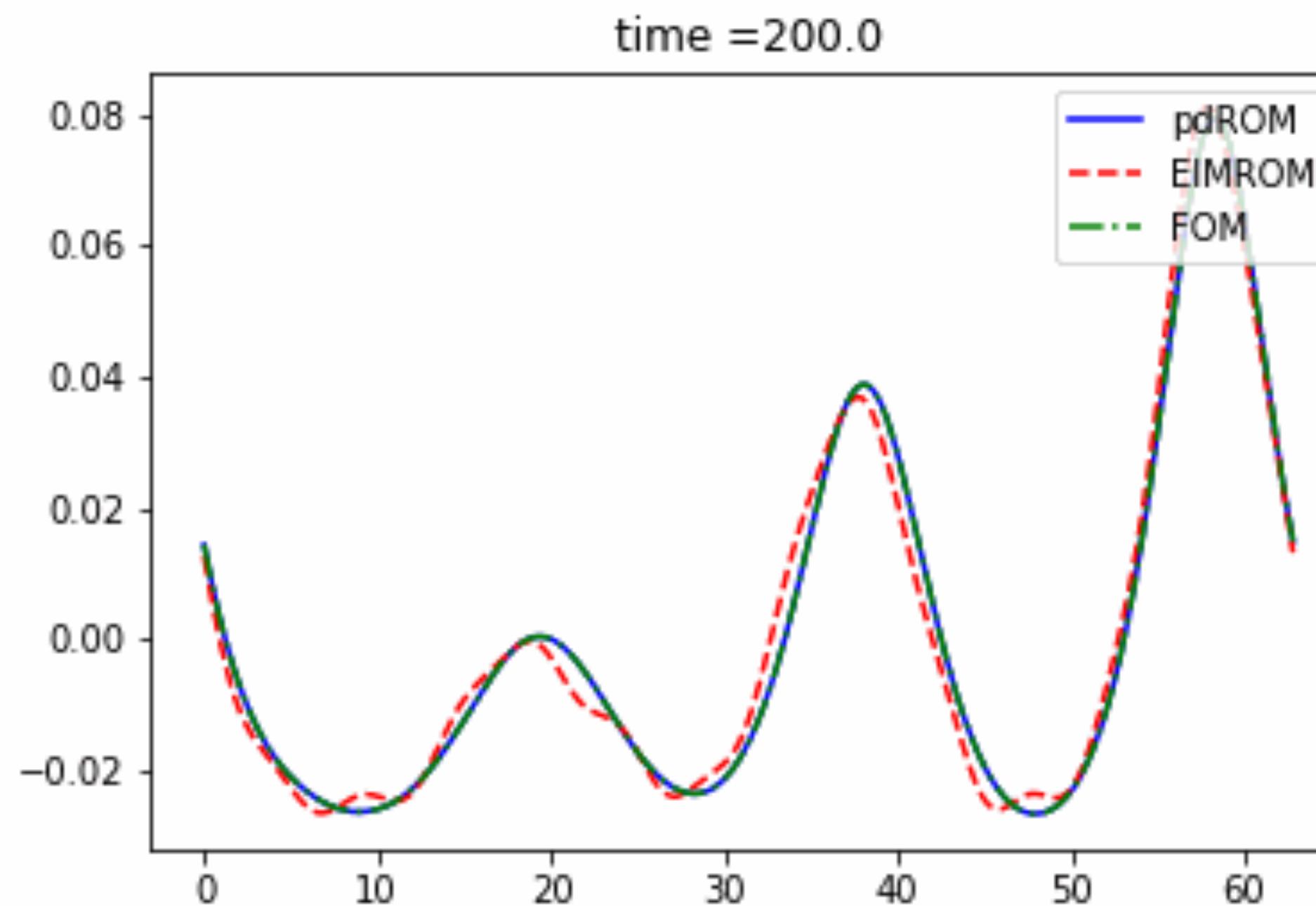
(D. Torlo/MR)



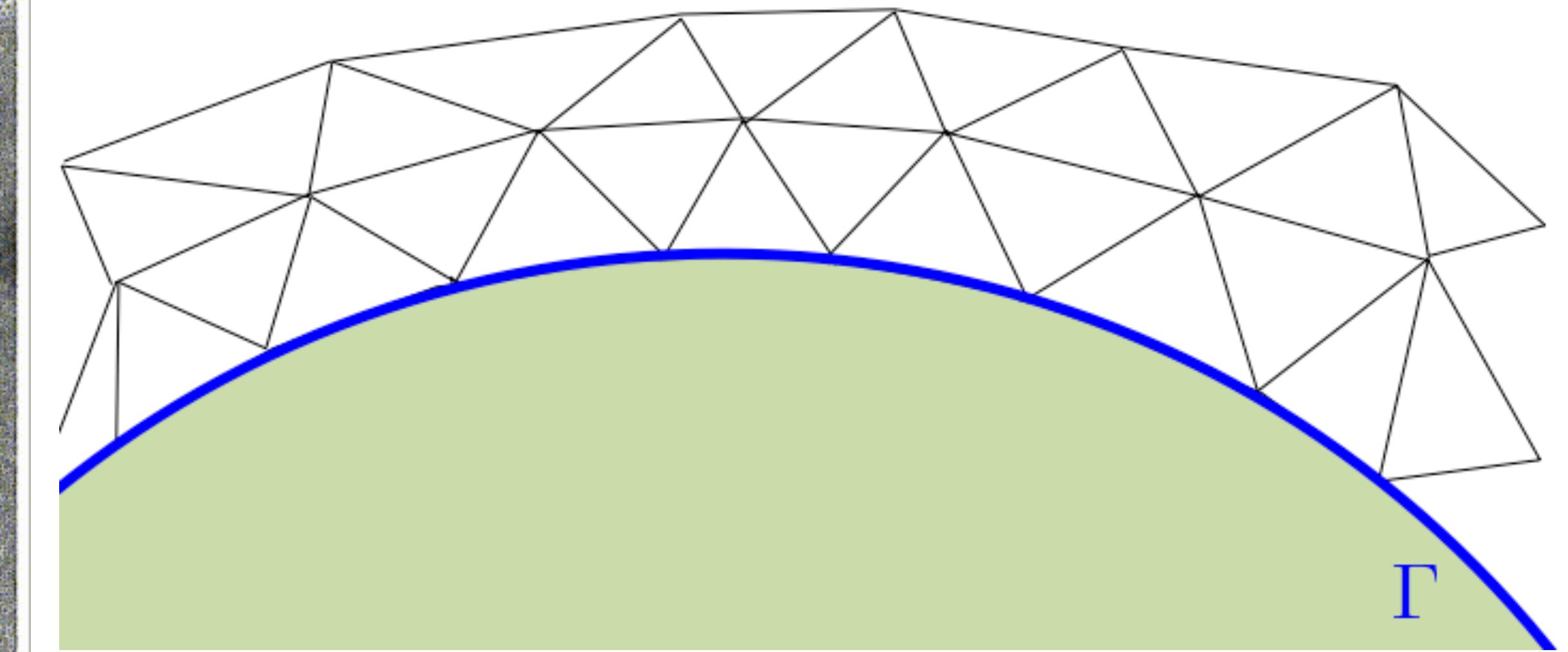
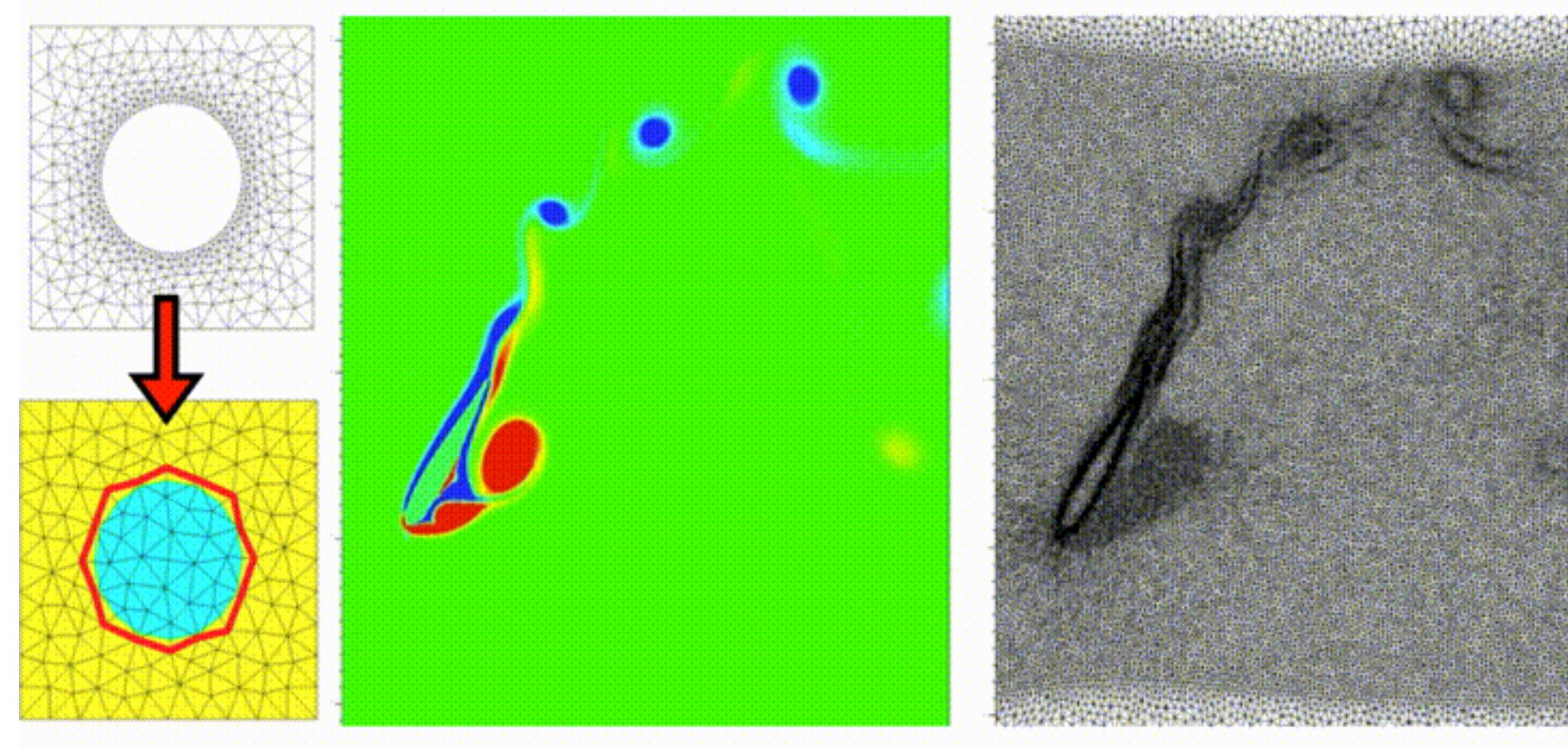
# Certified Adaptive discRete moDels for robust simulAtions of coMplex fLOws with Moving fronts

KdV/BBM model: **PDE-ROM vs ROM**

(D. Torlo/MR)



# Certified Adaptive discRete moDels for robust simulAtions of coMplex fLOws with Moving fronts



$$-\Delta u = f$$

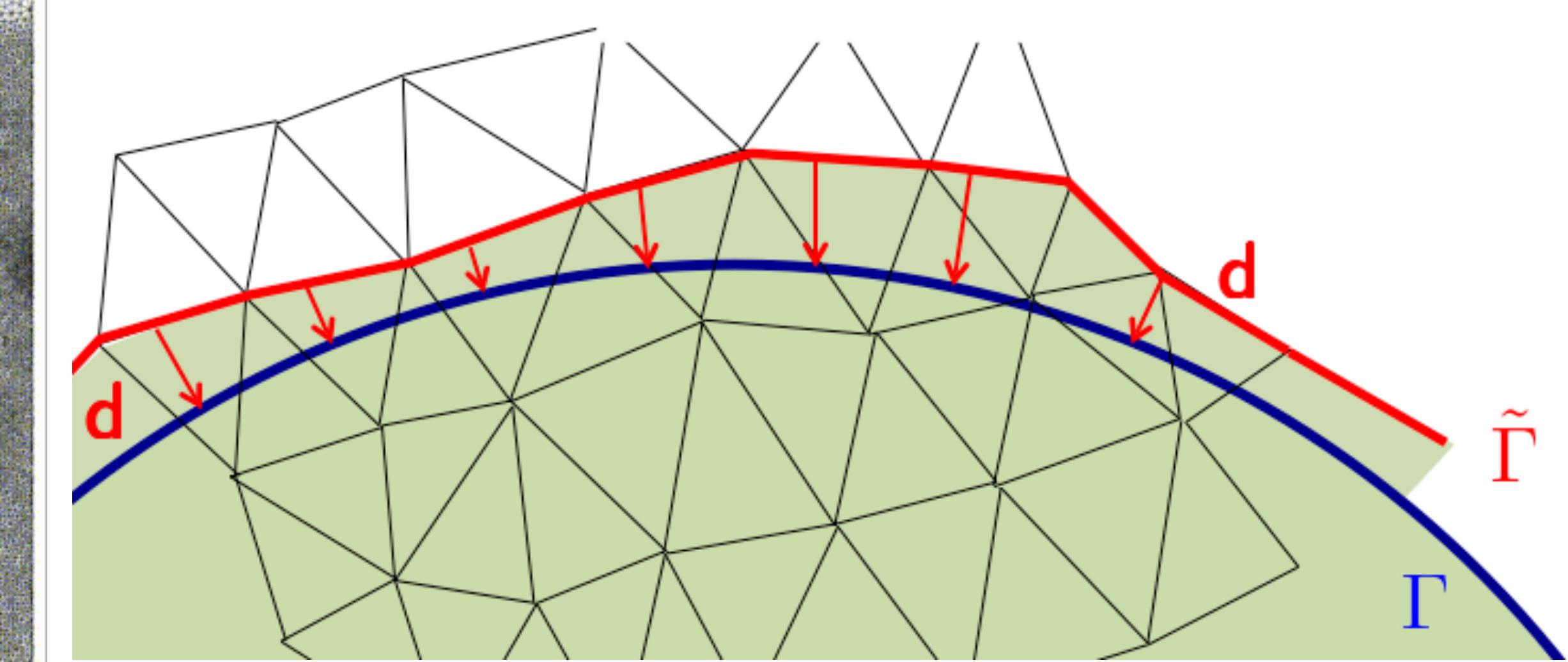
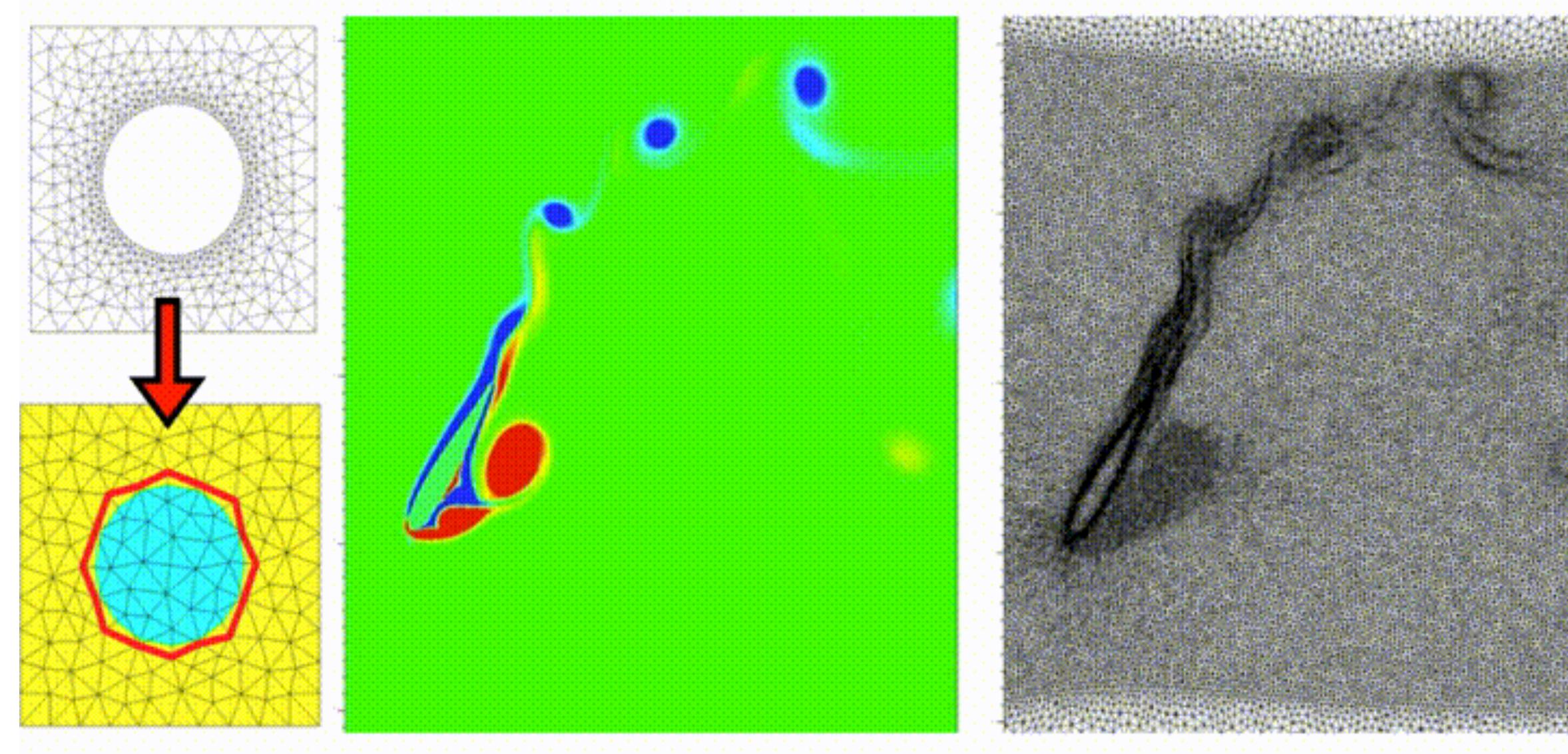
$$u = g + \mathcal{O}(\mu) \quad \text{on } \Gamma$$

**Modeling error**

Turbulence and/or heat transfer

## Embedded geometries, turbulence and heat transfer

# Certified Adaptive discRete moDels for robust simulAtions of coMplex fLOws with Moving fronts



$$-\Delta u = f$$

Discretization error  
geometry and mesh

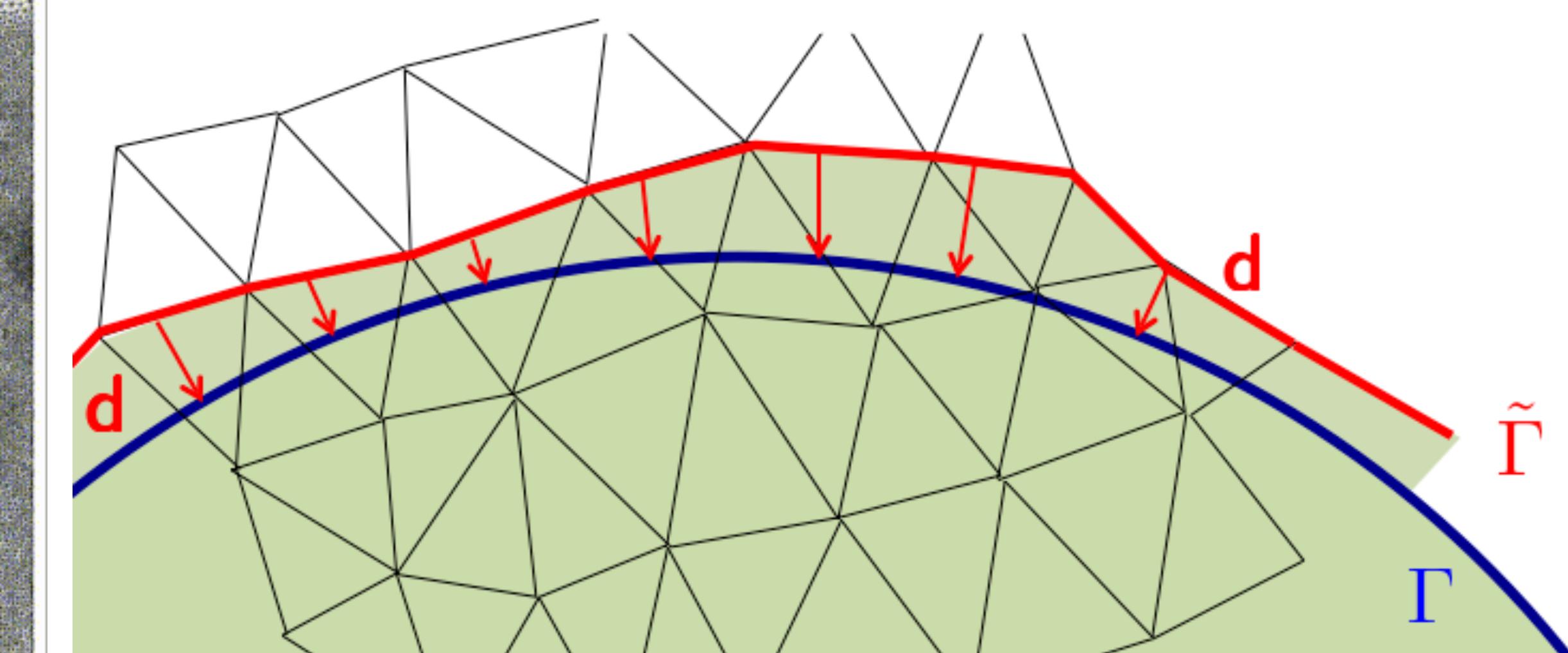
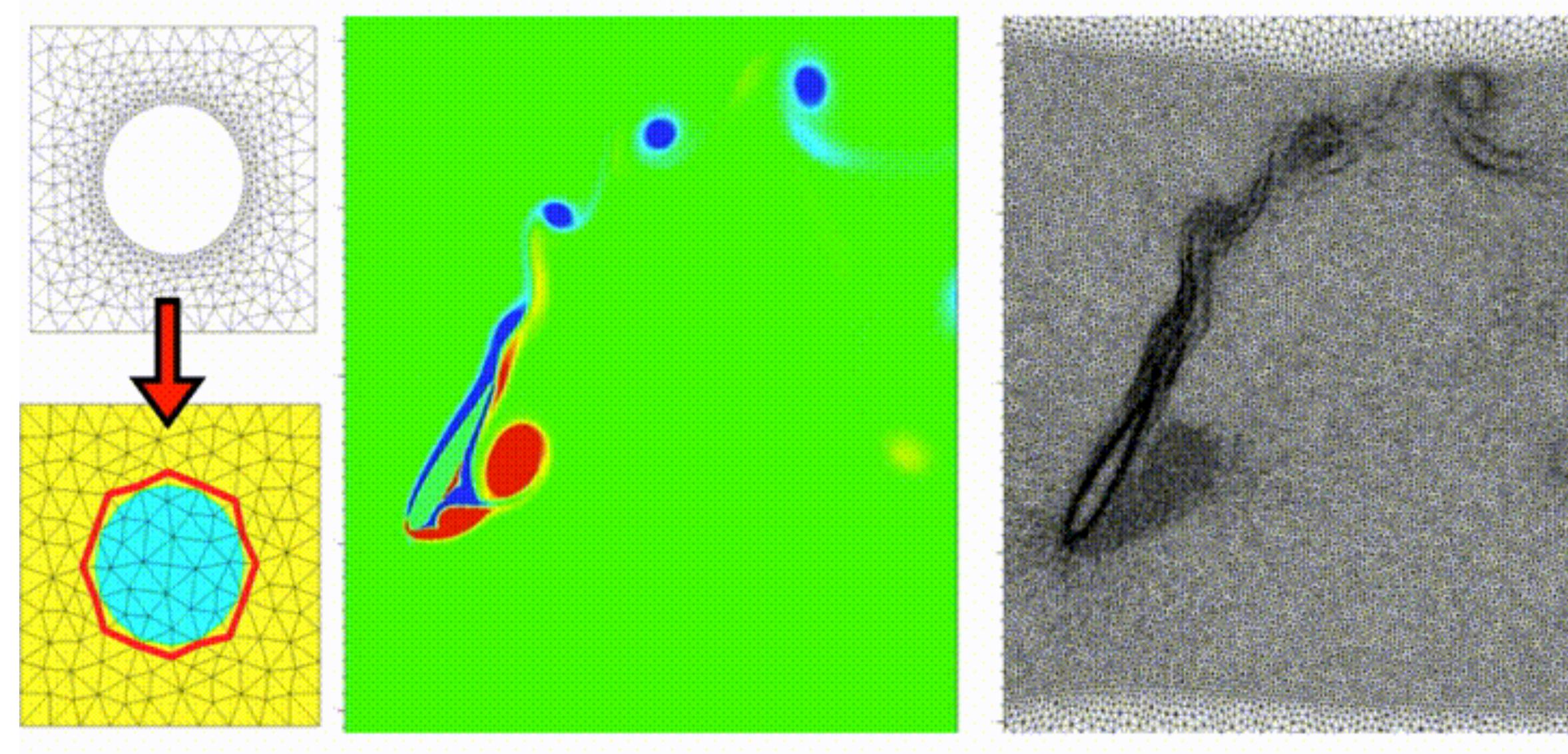
$$u = g + \mathcal{O}(\mu) + \tilde{F}_{\text{corr}}^{\Gamma}(d) \text{ on } \tilde{\Gamma}$$

Modeling error

Turbulence and/or heat transfer

## Embedded geometries, turbulence and heat transfer

# Certified Adaptive discRete moDels for robust simulAtions of coMplex fLOws with Moving fronts



$$-\Delta u = f$$

$$u = g + \mathcal{O}(\mu) + \tilde{F}_{\text{corr}}^{\Gamma}(d) + \epsilon_{\text{ML}} \quad \text{on } \tilde{\Gamma}$$

Discretization error  
geometry and mesh

Modeling error

Turbulence and/or heat transfer

Model learning error

Data (experiments, HF simulations) + machine learning

## Embedded geometries, turbulence and heat transfer

## **Lookout on possible evolutions:**

some MOR for small scales and in embedded moving domains

Discussions CARDAMOM/MEMPHIS

- Projet RNA (Parisot-Bergmann-MR)
- PhD ONERA Chair (Beaugendre-Bergmann-AI)
- Discussions on PDE-MOR vs registration (Taddei, Torlo, MR)
- Discussions on possible AEx MOR-Mesh adaptation/deformation