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## A mathematical model for indirectly transmitted diseases between two host populations

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## ABSTRACT

This talk fits into the general setting of invasion and persistence of parasites through spatially distributed host populations. We consider a mathematical model for the indirect transmission via a contaminated environment of a microparasite between two spatially distributed host populations having non coincident spatial domains. The parasite is benign in a first population and lethal in the second one.

Various heterogeneities are included in our model: spatially variable carrying capacities as well as temporal oscillations in carrying capacities. Global existence results are given for the resulting reaction-diffusion system coupled with an ordinary differential equation. Then, invasion and persistence of the parasite are studied. The impact of the parasite on the second host population is also assessed.

A simplified model for the transmission of a hantavirus from bank vole to human populations is then analysed.

This is a multidisciplinary work with D. Pontier (University Lyon1), W.-E. Fitzgibbon (University of Houston), F. Marpeau & C. Wolf (Bordeaux), F. Sauvage (Lyon).

**Key Words:** indirectly transmitted disease, reaction diffusion systems, global existence, invasion and persistence.

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